## Algorithmic Trends Homework 1

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The homework is due on 26/03/2014.

## Problem 1

Let G = (V, E) be an directed graph with two fixed vertices s and t. Propose an algorithm that computes the maximum number of vertex disjoint paths from s to t. The vertices s and t can be shared on these paths. Hint: Reduce the problem to the maximum matching problem.

## Problem 2

Let G = (V, E) be a graph. Assume that you are given an algorithm A that checks for every pair of nodes  $x, y \in V$  whether there exists a perfect matching in G - x - y. Show how to use this algorithm to multiply two boolean matrices of size  $|V| \times |V|$  in asymptotically the same time as the running time of A?

## Problem 3

Let G be a graph. Prove that if a vertex set  $S \subseteq V(G)$  is covered by some matching, then there exists a maximum size matching that covers S.